

10<sup>th</sup> April nuclear physics discussion solutions

① No. of neutrons release per fission  $\bar{\nu}$   
 $\bar{\nu}$  for  $U^{235} = 2.48$

$\bar{\nu}$  for  $Pu^{239} = 2.92$

As neutrons from fission escape from surface:  
lesser the surface area lesser the chances  
of escape from material.

Sphere has least surface area for  
given volume.

' $\bar{\nu}$ ' more means lesser the critical mass  
for given shape.

$\therefore Pu^{239}$  sphere has least critical mass.

Ans: 2 plane sheet has largest  
surface area  $\therefore$  larger  
critical mass

② Nuclear forces are short range hence  
includes only neighbours. If electromagnetic  
forces were absent on a particular  
nucleon strong nuclear force after reaching  
certain value remains constant.

$\therefore B \cdot E / \text{nucleon}$  first increases then remain  
constant. Due to electromagnetic forces  
 $B \cdot E / \text{nucleon}$  after reaching maximum,  
starts decreasing.

③  $A \rightarrow B + C$  to conserve momentum  
(free) energy generated due to  
mass decrease  
 $\therefore m_A > (m_B + m_C)$

If 'A' were bound in nucleus,  $m_A$  can be less  
as internally energy  $\underline{m \Delta m c^2}$   
change can occur.

(4) Any radioactive nucleus has lifetime zero to infinity.

Law of disintegration is valid only when sample contains large number.

$$(5) R_1 = \lambda N_1 \Rightarrow N_1 = \frac{R_1}{\lambda}$$

$$R_2 = \lambda N_2 \Rightarrow N_2 = \frac{R_2}{\lambda}$$

$$\begin{aligned} \therefore \text{No. of disintegration} \\ \text{or No. of } \beta^- \text{ or No. of } \bar{\nu} &= N_1 = N_2 = \frac{1}{\lambda} (R_1 + R_2) \\ &= \frac{1}{\ln 2} (R_1 + R_2) \end{aligned}$$

(6) When no. of radioactive nuclei reaches maximum

$$P = \lambda N \quad N_{\text{max}} = \frac{P}{\lambda}$$

$$\frac{dN}{dt} = P - \lambda N$$

at

$$\text{for } N_{\text{max}} \quad \frac{dN}{dt} = 0$$

upto that time

$$\text{Produced nuclei} = Pt$$

$$\begin{aligned} \therefore \text{No. of nuclei disintegrated} \\ = Pt - \frac{P}{\lambda} \end{aligned}$$

$\therefore$  Total Energy released

$$= P \left( t - \frac{1}{\lambda} \right) E_0$$

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⊙ M

$$P = \frac{h}{\lambda}$$

⊙

$m_{\alpha}$

$$KE_{\alpha} = \frac{h^2}{2m_{\alpha}\lambda^2}$$

$$P = \frac{h}{\lambda}$$

⊙

$m_{\beta}$

$$KE_{\beta} = \frac{h^2}{2m_{\beta}\lambda^2}$$

$$[M - (m_{\alpha} + m_{\beta})]c^2 = \frac{h^2}{2\lambda^2} \left( \frac{1}{m_{\alpha}} + \frac{1}{m_{\beta}} \right)$$

8 Ans 2 B3

neutrino rest mass is negligibly small but not zero

for neutrino spin and momentum are in opposite directions

but for  $\bar{\nu}$  they are in same direction.

$$9 \quad N_0 = \frac{m}{M} N_A \quad \alpha = N_0 e^{-2} = \frac{N_0}{e^2}$$

$$\therefore \text{Number of disintegrations} = N_0 - N$$
  
$$\text{(no. of } \alpha \text{ particles emitted)} = N_0 \left( 1 - \frac{1}{e^2} \right)$$

10 If Activity ratio of  $\alpha$  and  $\beta = x : y$   
then probability of getting  $\alpha$  and probability  
of getting  $\beta$  at an instant  
are  $\frac{x}{x+y}$  and  $\frac{y}{x+y}$  respectively